

## Optimal Inventory Policy for Two-echelon Remanufacturing

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## Introduction

- OBJECTIVE: Identify the inventory policies that will fit a remanufacturing environment:
- sequential disassembly and selection processes
- random yield in each process
- known demand
- ASSUMPTION: There is no shortage of used goods to feed the process:
- plentiful stock of used goods
- uncertainty is generated by the wear state


## Some related literature

|  | Single Process |  | Multi Process |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Constant Process Yield | Random Process Yield | Constant Process Yield | Random Process Yield |
| Constant Demand | $\begin{gathered} \text { Harris } \\ 1913 \end{gathered}$ | various | Clark, Scarf 1960 |  |
| Random Demand | various | various | DeBodt and Graves 1985 |  |

## Used tires flow in the retreading process

## Value adding processes



## Electric Components



# Material flow of complex equipment refurbishing process 



## Multi-Echelon Inventory Process



## Financial and Physical Stock



## Financial and Physical Holding Cost



## Financial and Physical Setup Cost



## Optimal Inventory Policy

Considering: $\left\{\begin{array}{c}n=\sqrt{\frac{E\left[p_{d}\right]\left(h_{f, r}-h_{p h, d}+h_{p h, r} E\left[p_{r}\right]\right)}{h_{f, d}+h_{p h, d} E\left[p_{d}\right]}} \frac{k_{d}}{k_{r}} \\ H(n)=h_{f, d}+\frac{E\left[p_{d}\right]}{n}\left(h_{p h, d}(n-1)+h_{f, r}+h_{p h, r} E\left[p_{r}\right]\right) \\ K(n)=\left(k_{d}+n k_{r}\right) E\left[1 / p_{d}\right] E\left[1 / p_{r}\right]\end{array}\right.$

$$
\text { Optimal Inventory Policy } \quad Q^{*}(n)=\sqrt{\frac{2 D K(n)}{H(n)}}
$$

## Example

Disassembly Process:
$\mathrm{k}_{\mathrm{d}}=\$ 30 /$ process
$\mathrm{h}_{\mathrm{f}, \mathrm{d}}=\$ 0.5 /$ unit-yr
$h_{\mathrm{ph}, \mathrm{d}}=\$ 2 /$ unit-yr
$\mathrm{p}_{\mathrm{d}}=\mathrm{U}[0.5,0.95]$
Repair Process:
$\mathrm{k}_{\mathrm{r}}=\$ 6 /$ process
$\mathrm{h}_{\mathrm{f}, \mathrm{r}}=\$ 4 / \mathrm{unit}-\mathrm{yr}$
$\mathrm{h}_{\mathrm{ph}, \mathrm{r}}=\$ 2 /$ unit-yr
$\mathrm{p}_{\mathrm{r}}=\mathrm{U}[0.75,0.95]$
D $=600$ units/yr


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$$
\begin{aligned}
& \mathrm{Q}^{*}=185 \text { units } \\
& \mathrm{n}^{*}=3
\end{aligned}
$$

